

Neutron Kinetics in Liquid-Fueled Nuclear Reactors
IUSSTF Symposium on Advanced Sensors and Modelling Techniques for
Nuclear Reactor Safety

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ILLINOIS



Outline

① Introduction

ARFC Research Group
Molten Salt Reactors

② Point Kinetics & TH Coupling

Point and Multi-point Kinetics

③ Spatial Kinetics & TH Coupling with Precursor Advection



Advanced Reactors and Fuel Cycles group (PI: Kathryn Huff)



**ANDREI
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FAIRHURST
AGOSTA**



**LOUIS
KISSINGER**



**TYLER
KENNELLY**



**ZOE
RICHTER**



**MATTHEW
KOZIOL**

Figure: Current undergraduate and graduate students.



Advanced Reactors and Fuel Cycles group (PI: Kathryn Huff)



ALEX LINDSAY



GAVIN RIDLEY



**SNEHAL
CHANDAN**

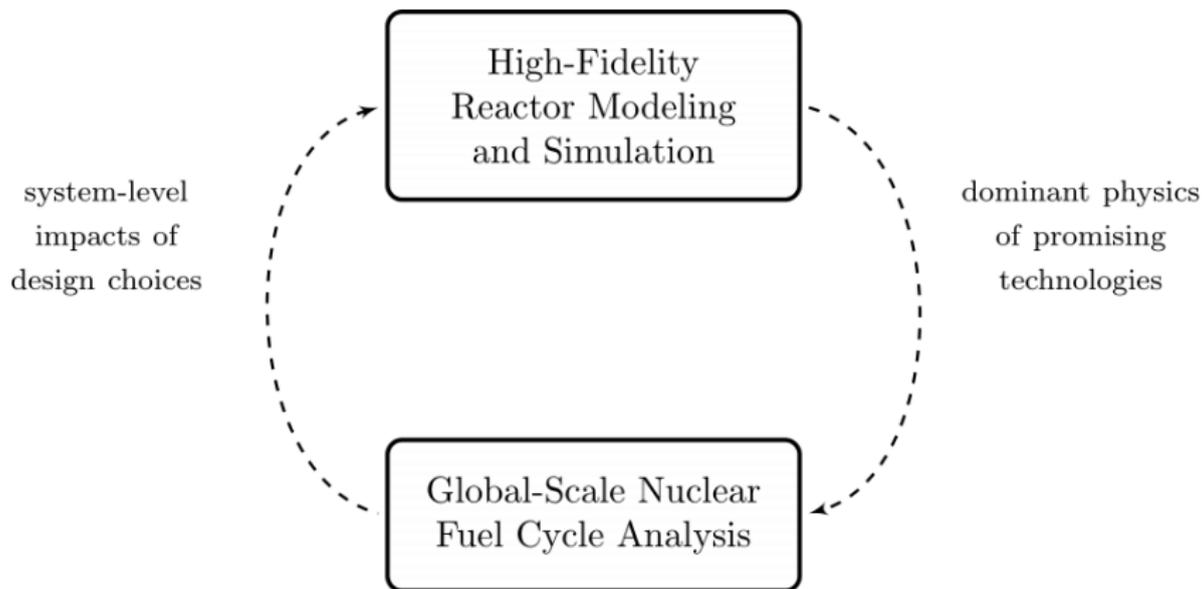


**ADITYA
BHOSALE**

Figure: Past ARFC Group members who contributed to this work.



Insights at Disparate Scales





Types of Molten Salt Reactors

Stationary Fuel

- Prismatic graphite block with TRISO fuel and coolant channels (e.g. FHR DR, TMSR-SF1). Clean salt coolant.
- Stationary TRISO pebble matrix (e.g. TMSR-SF)

Mobile Fuel

- Mobile solid fuel elements, such as pebbles. Clean salt coolant. (e.g. PB-FHR/Kairos)
- Non-circulating fuel salt, “can-type”. (e.g. Terrapower MCFR)
- Circulating fuel salt “pool-type”. (e.g. MSRE, MSBR, MSFR, Terrestrial MSR, TAP MSR, etc.)



Stationary Solid Fuel

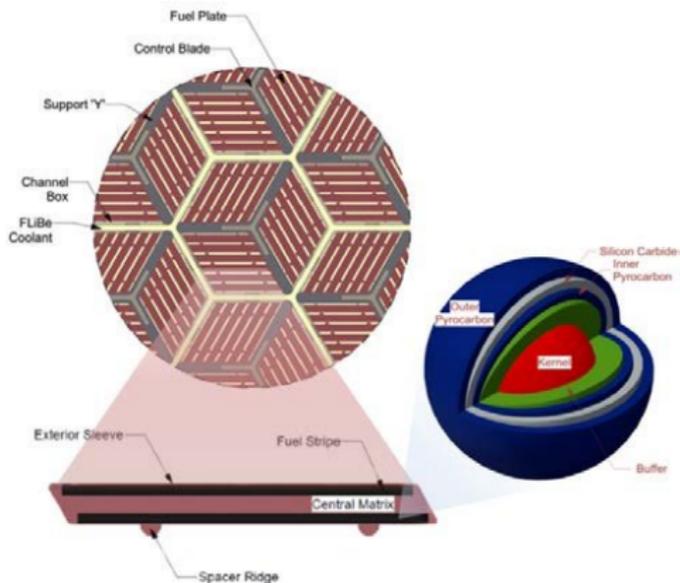


Figure: The AHTR [4] is an example of a fluoride salt cooled reactor design fueled by a **stationary, solid** prismatic graphite TRISO compacts, and cooled by clean fluoride salt. Image source [5].

Mobile Solid Fuel

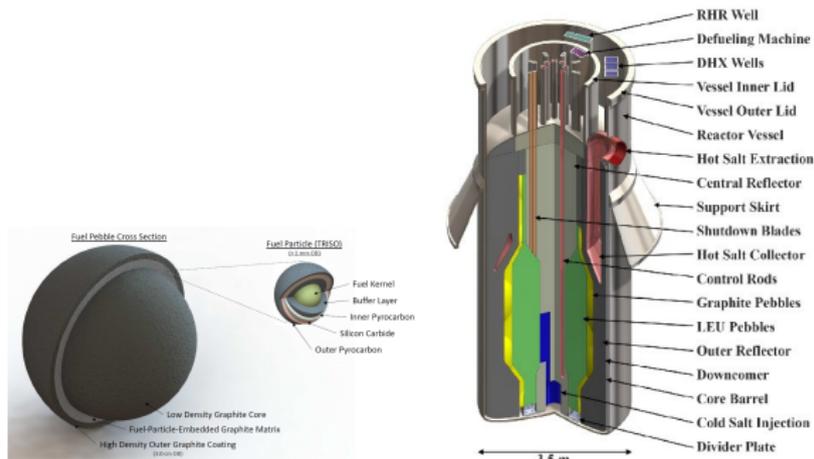


Figure: The PB-FHR is an example reactor design fueled by **solid, mobile** graphite pebbles, with TRISO particles embedded in them. Image source [1].



Mobile, Non-Circulating, Liquid Fuel

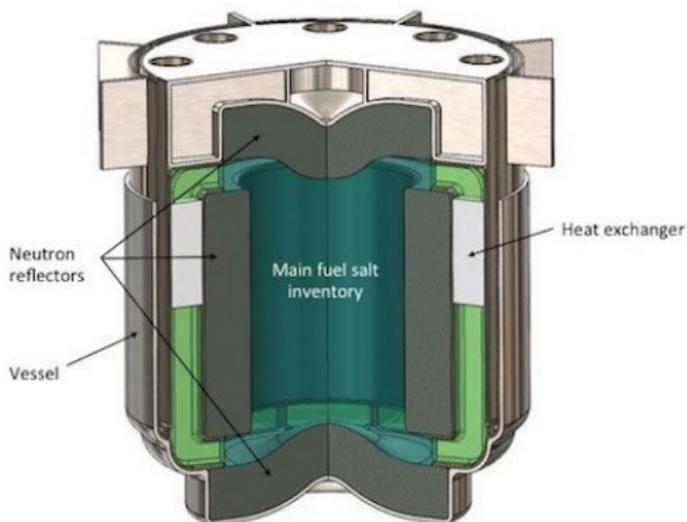


Figure: The MCFR from TerraPower is an example reactor design with **liquid, mobile, non-circulating** chloride salt fuel. Image source [12, 2].



Mobile, Circulating, Liquid Fuel

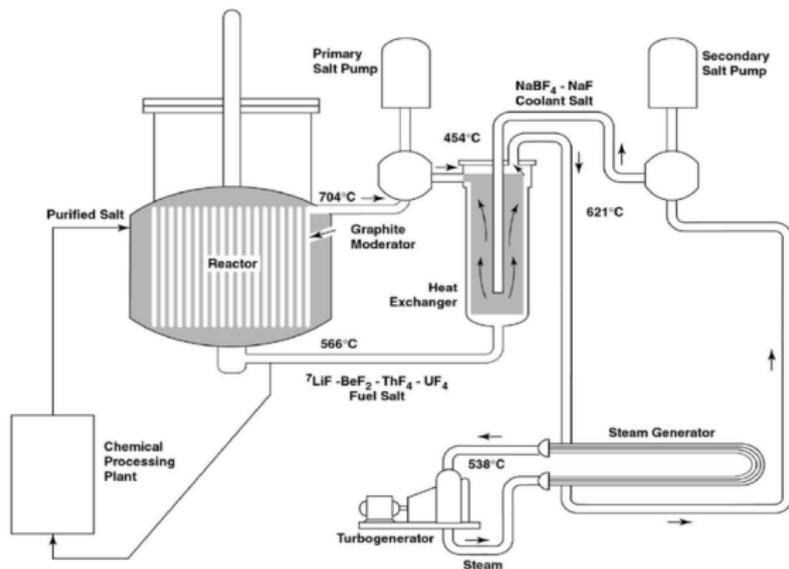


Figure: The MSBR [8] is an example reactor design with **liquid, mobile, circulating** fluoride salt fuel, including breeding behavior due to varying channel shapes and sizes. Image source [9].



Why Molten Salt Reactors?

Main advantages of liquid-fueled Molten Salt Reactors (MSRs) [3]

- 1 High coolant temperature (600-750°C).
- 2 Various fuels can be used (^{235}U , ^{233}U , Thorium, U/Pu).
- 3 Increased inherent safety.
- 4 High fuel utilization \Rightarrow less nuclear waste generated.
- 5 Online reprocessing and refueling.

Main advantages of MSBR [8]

- 1 Produces more fissile material than it consumes (breeding ratio 1.06).
- 2 Thorium cycle limits plutonium and minor actinides.
- 3 Could transmute spent fuel from existing Nuclear Power Plant (NPP).

Challenges in Liquid-Fueled Reactor Simulation

- 1 Contemporary burnup codes cannot treat fuel movement.
- 2 Neutron precursor locations drift before neutron emission.
- 3 Operational and safety parameters change during reactor operation.
- 4 Neutronics and thermal hydraulics are tightly interdependent.

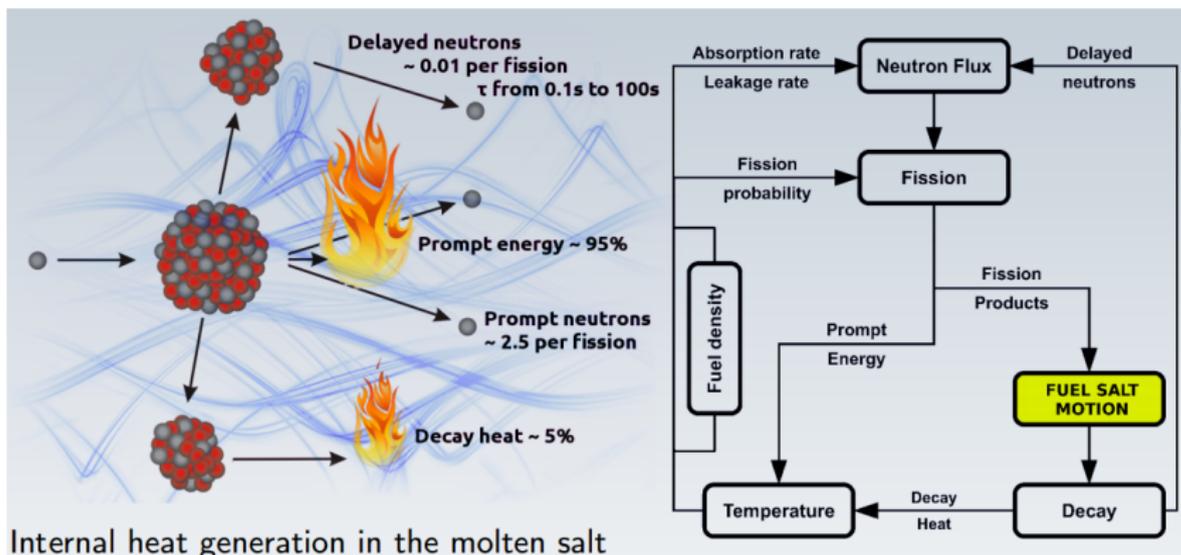


Figure: Challenges in simulating MSRs (Image courtesy of Manuele Aufiero, 2012).



Approaches

Point Reactor Kinetics [6]

Only appropriate for stationary or nearly stationary fuels.

Simulation of online reprocessing and depletion (SaltProc)[10, 11]

- 1 Create high-fidelity full-core neutronics model of the core neutronics can be necessary for reducing compounding error.
- 2 SaltProc wraps SERPENT monte carlo neutron transport for simulation of liquid fuel reprocessing.
- 3 Enables day-to-day resolution of neutronics and reprocessing modeling over many decades of depletion and fuel cycle performance.

Multiphysics simulation of MSR (Moltres)[7]

- 1 Steady-state and transient coupling of neutron fluxes, precursor drift, and thermal-hydraulics.
- 2 Incorporates advective movement of delayed neutron precursors.
- 3 2D axisymmetric and 3D geometries supported.



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PyRK: Python for Reactor Kinetics

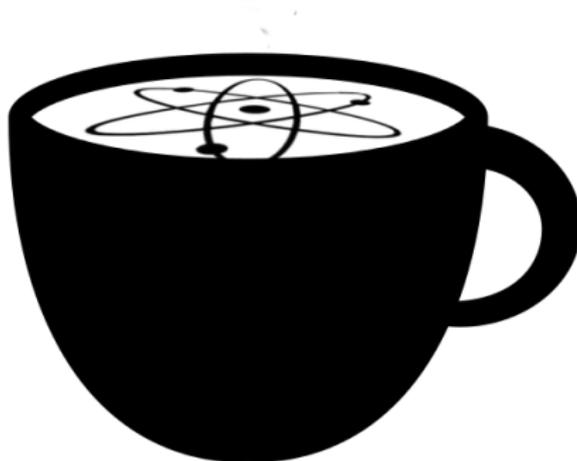


Figure: Special purpose reactor kinetics python tool (<https://github.com/pyrk/pyrk>) [6].
Research software for simple PRKE: *caveat emptor*.

- Multiple precursor groups (j groups)
- Multiple decay heat groups (k groups)
- Lumped Parameter thermal hydraulics model
- Optional 1-D conduction in pebble fuel compacts
- Object-oriented, geometry and material agnostic framework



Point Reactor Kinetics

$$p = \text{reactor power} \quad (1)$$

$$\rho(t, T_{fuel}, T_{cool}, T_{mod}, T_{refl}) = \text{reactivity} \quad (2)$$

$$\beta = \text{fraction of neutrons that are delayed} \quad (3)$$

$$\beta_j = \text{fraction of delayed neutrons from precursor group } j \quad (4)$$

$$\zeta_j = \text{concentration of precursors of group } j \quad (5)$$

$$\lambda_{d,j} = \text{decay constant of precursor group } j \quad (6)$$

$$\Lambda = \text{mean generation time} \quad (7)$$

$$\omega_k = \text{decay heat from FP group } k \quad (8)$$

$$\kappa_k = \text{heat per fission for decay FP group } k \quad (9)$$

$$\lambda_{FP,k} = \text{decay constant for decay FP group } k \quad (10)$$

$$T_i = \text{temperature of component } i \quad (11)$$



Point Reactor Kinetics

$$\frac{d}{dt} \begin{bmatrix} \rho \\ \zeta_1 \\ \cdot \\ \zeta_j \\ \cdot \\ \zeta_J \\ \omega_1 \\ \cdot \\ \omega_k \\ \cdot \\ \omega_K \\ T_i \\ \cdot \\ T_l \end{bmatrix} = \begin{bmatrix} \frac{\rho(t, T_i, \dots) - \beta}{\Lambda} \rho + \sum_{j=1}^{j=J} \lambda_{d,j} \zeta_j \\ \frac{\beta_1}{\Lambda} \rho - \lambda_{d,1} \zeta_1 \\ \cdot \\ \frac{\beta_j}{\Lambda} \rho - \lambda_{d,j} \zeta_j \\ \cdot \\ \frac{\beta_J}{\Lambda} \rho - \lambda_{d,J} \zeta_J \\ \kappa_1 \rho - \lambda_{FP,1} \omega_1 \\ \cdot \\ \kappa_k \rho - \lambda_{FP,k} \omega_k \\ \cdot \\ \kappa_{kP} \rho - \lambda_{FP,k} \omega_k \\ f_i(\rho, C_{p,i}, T_i, \dots) \\ \cdot \\ f_l(\rho, C_{p,l}, T_l, \dots) \end{bmatrix} \quad (12)$$



Lumped Parameter Heat Transfer

The heat flow out of body i is the sum of surface heat flow by conduction, convection, radiation, and other mechanisms to each adjacent body, j :

$$Q = Q_i + \sum_j Q_{ij} \quad (13)$$

$$= Q_i + \sum_j \frac{T_i - T_j}{R_{th,ij}} \quad (14)$$

$$\dot{Q} = \text{total heat flow out of body } i \text{ [} J \cdot s^{-1} \text{]} \quad (15)$$

$$Q_i = \text{other heat transfer, a constant [} J \cdot s^{-1} \text{]} \quad (16)$$

$$T_i = \text{temperature of body } i \text{ [} K \text{]} \quad (17)$$

$$T_j = \text{temperature of body } j \text{ [} K \text{]} \quad (18)$$

$$j = \text{adjacent bodies [-]} \quad (19)$$

$$R_{th} = \text{thermal resistance of the component [} K \cdot s \cdot J^{-1} \text{]}. \quad (20)$$



PB-FHR Example

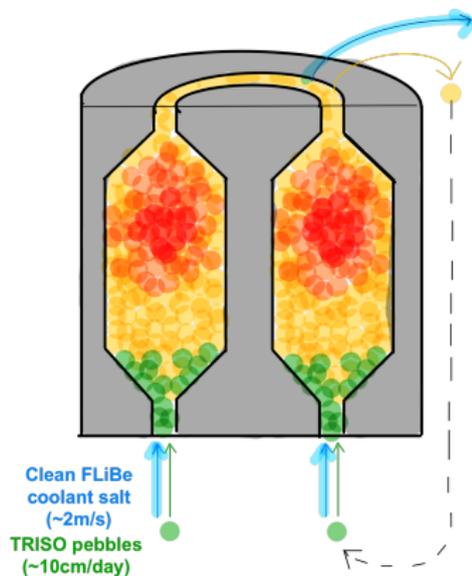


Figure: The pebble fuel can be assumed approximately stationary, as their movement is not comparable to the longest precursor decay times.



Point Reactor Kinetics

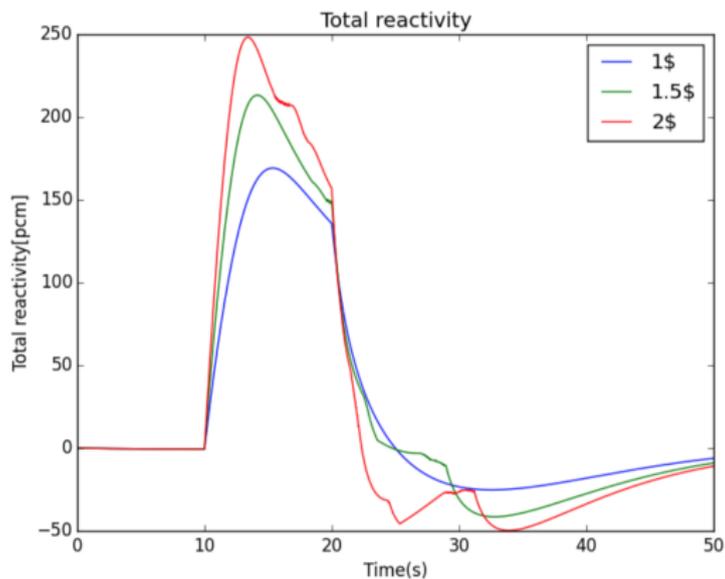


Figure: Total reactivity during ramped reactivity insertion as a function of inserted reactivity [13].



PB-FHR Example

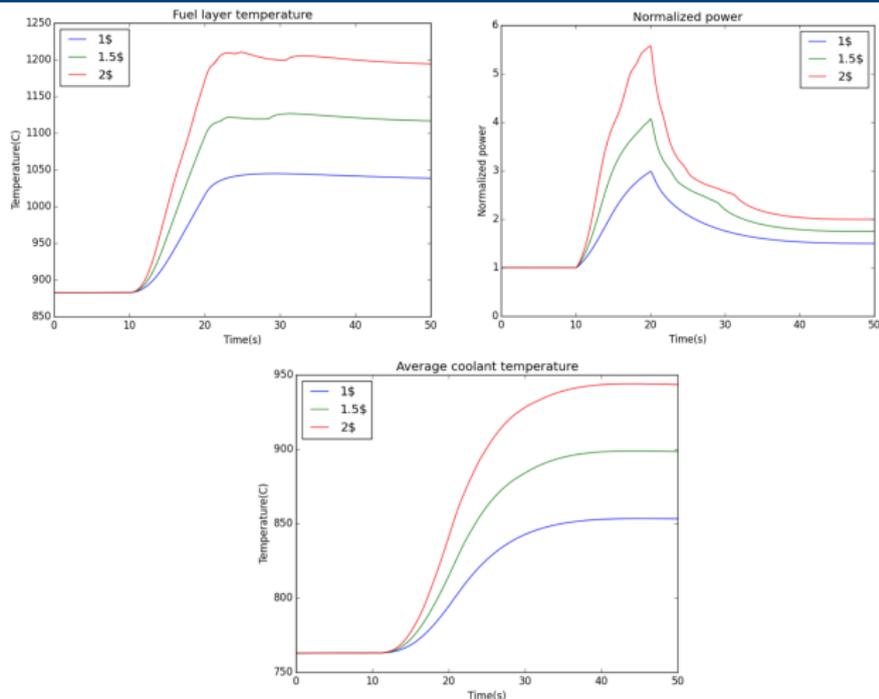


Figure: Average fuel temperature (left) and average normalized core power (right) during a ramp reactivity insertion in the PB-FHR [13].



Point Reactor Kinetics

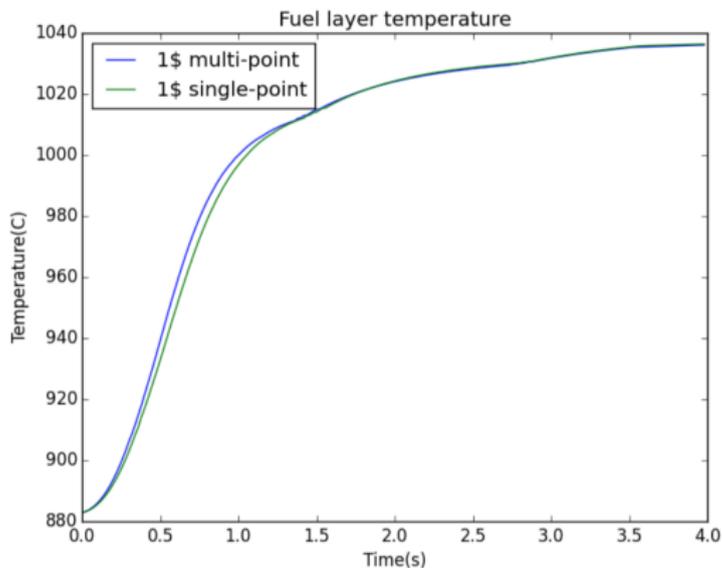


Figure: Fuel temperature rise following 1\$ ramp reactivity insertion, calculated with multipoint and single point kinetics in PyRK [13].



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Full-core SERPENT model of MSBR

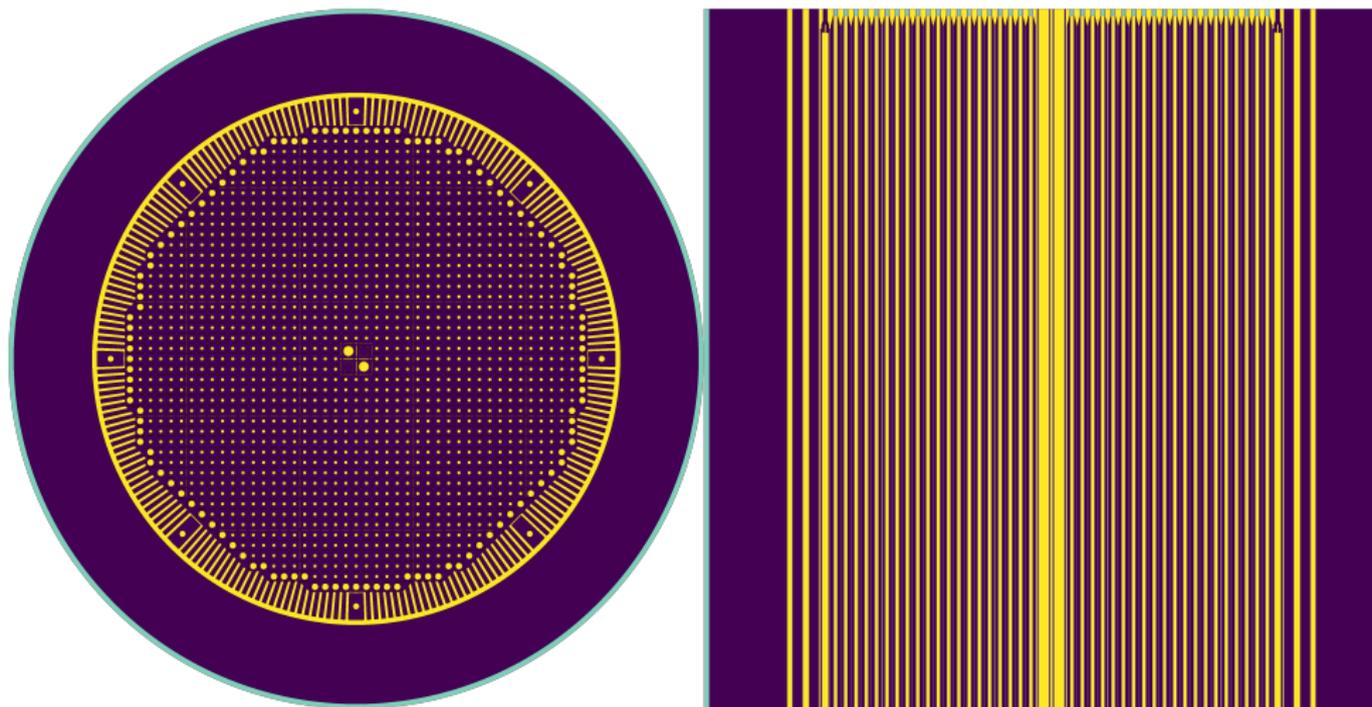


Figure: Plan (left) and elevation (right) view of MSBR model.

Core Zone II

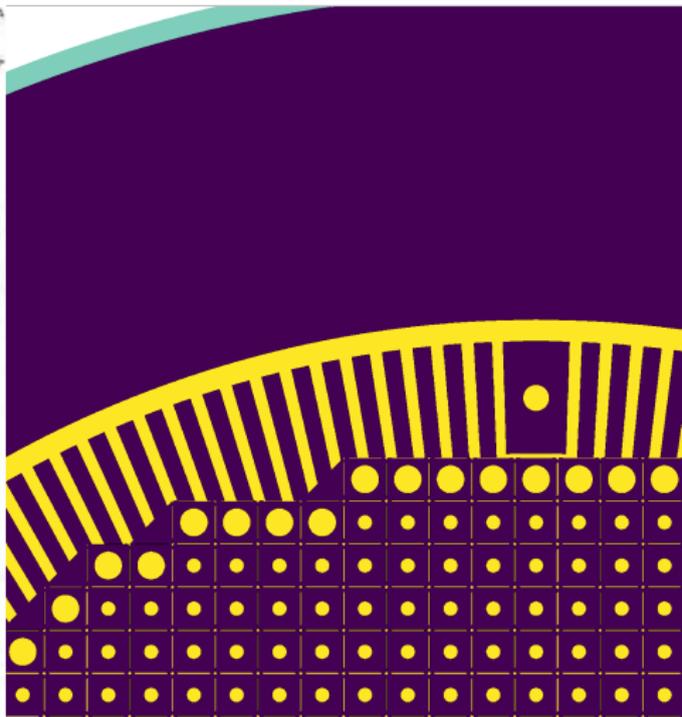
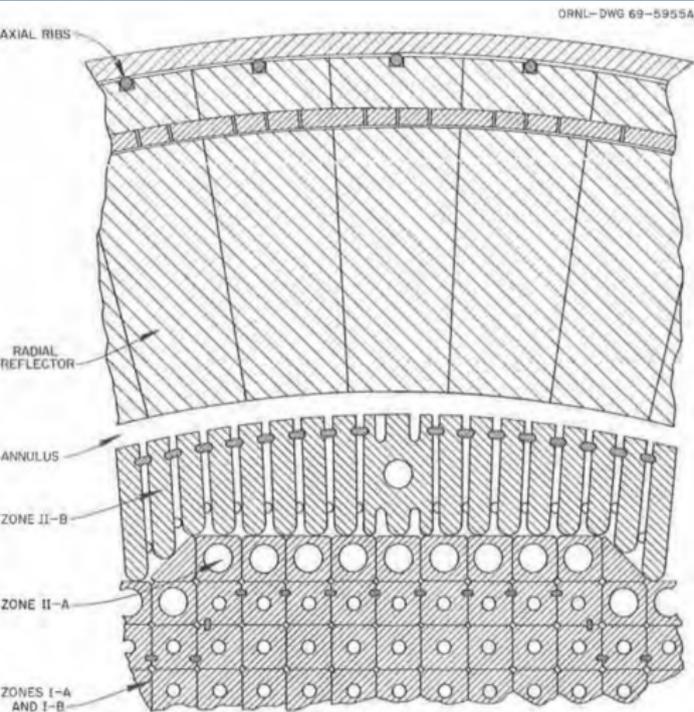


Figure: Detailed plan view of graphite reflector and moderator elements.

Moderator element geometry (Zone I)

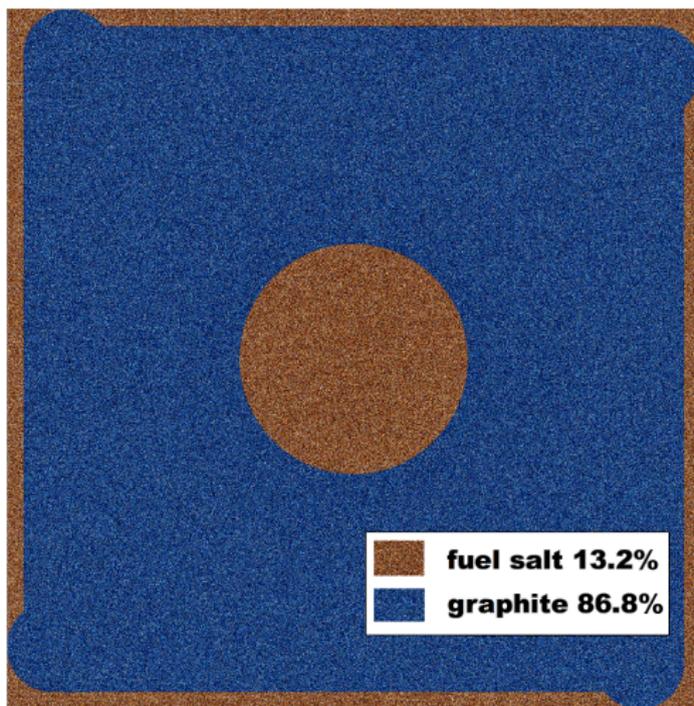
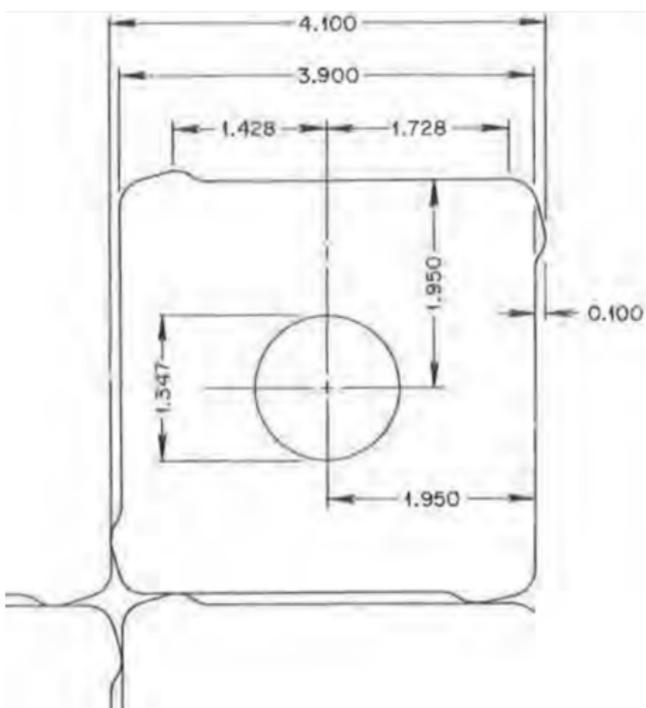


Figure: Molten Salt Breeder Reactor Zone I unit cell geometry from the reference [8] (left) and SERPENT 2 (right).

Online reprocessing method

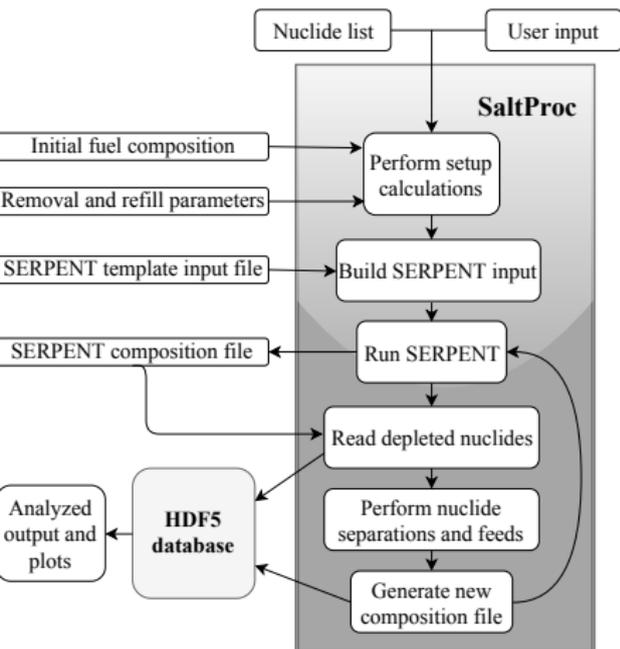


Figure: Flow chart for the SaltProc.

SaltProc capabilities

- Remove specific isotopes from the core with specific parameters (reprocessing interval, mass rate, removal efficiency)
- Add specific isotopes into the core
- Maintain constant number density of specific isotope in the core
- Store stream vectors in an HDF5 database for further analysis or plots
- Generic geometry: an infinite medium, a unit cell, a multi-zone simplified assembly, or a full-core

Online reprocessing method

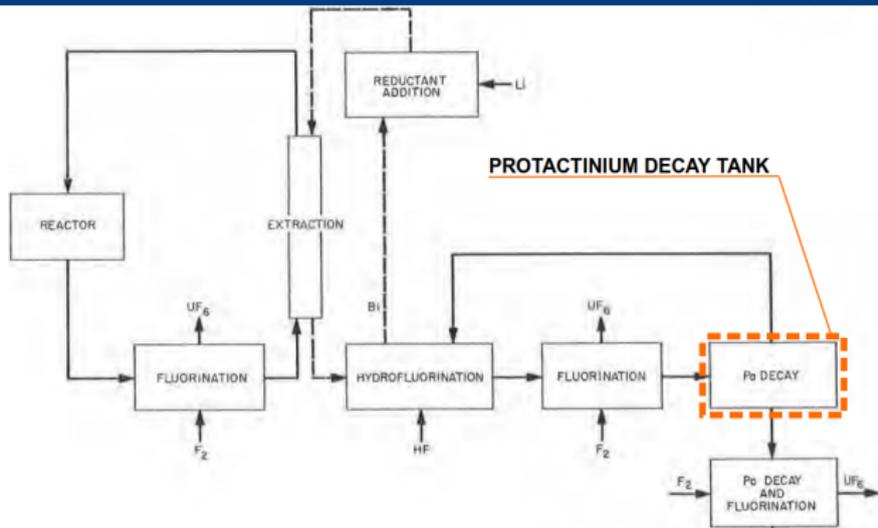
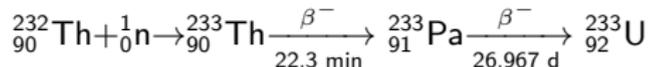


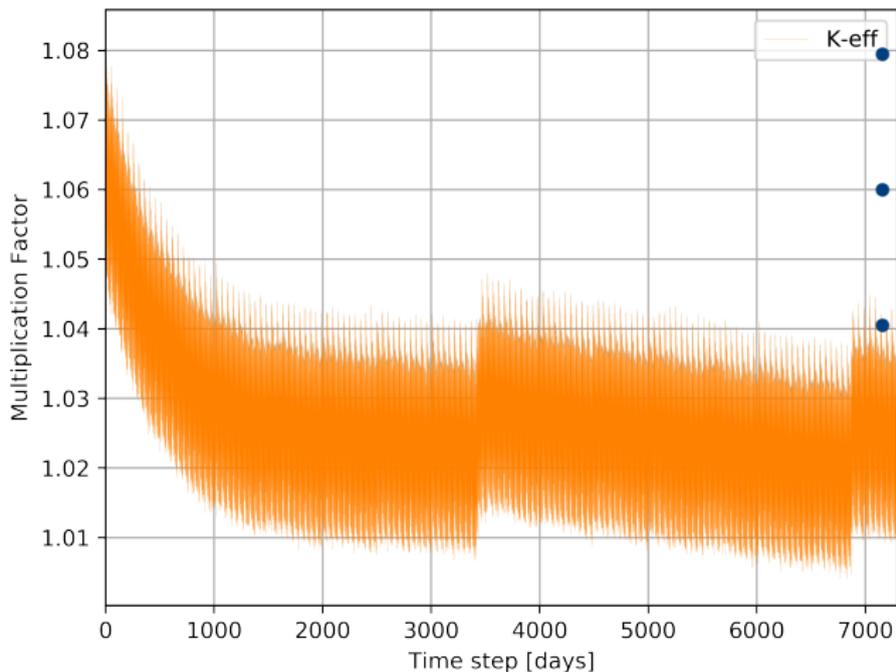
Figure: Protactinium isolation with uranium removal by fluorination [8].

Online reprocessing approach

- Continuously removes all poisons, noble metals, and gases.
- ^{233}Pa is continuously removed from the fuel salt into a decay tank.



Effective multiplication factor for full-core MSBR model



- Strong absorbers (^{233}Th , ^{234}U) accumulating in the core
- Fissile materials other than ^{233}U are bred into the core (^{235}U , ^{239}Pu)
- The multiplication factor stabilizes after approximately 6 years

Figure: k_{eff} during a 20 years depletion simulation.

Power and breeding distribution

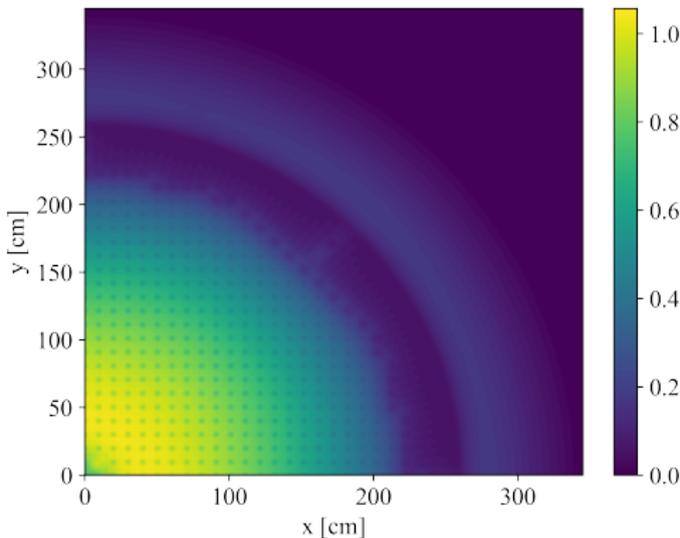


Figure: Normalized power density

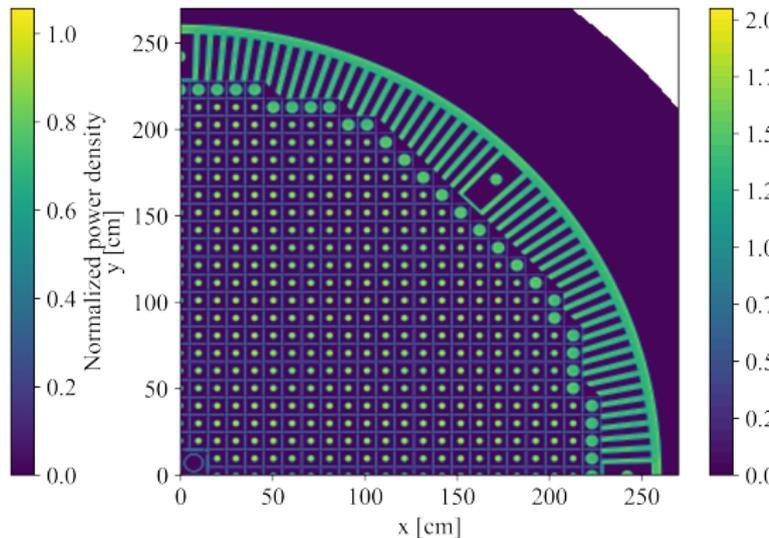
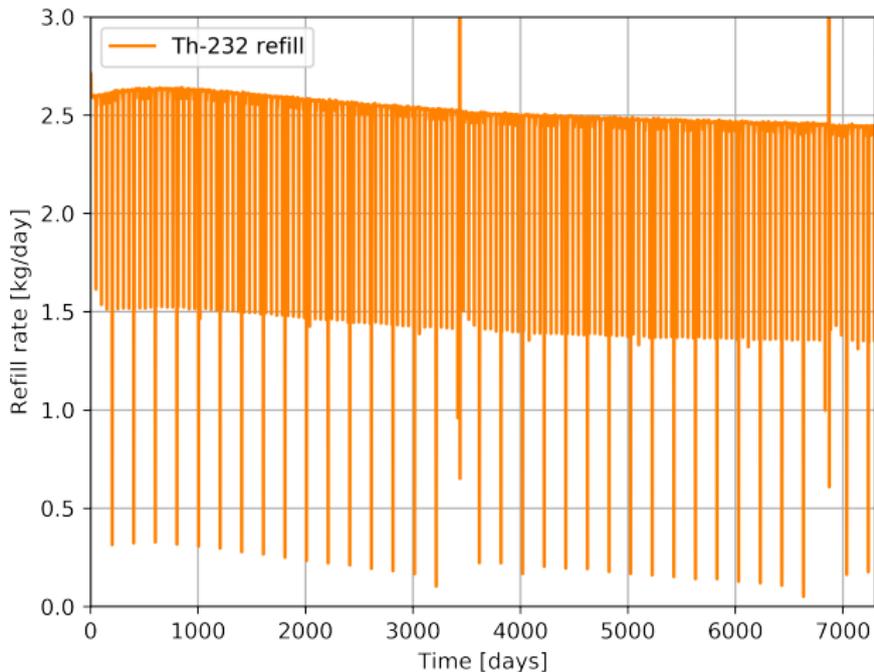


Figure: ^{232}Th neutron capture reaction rate normalized by total flux

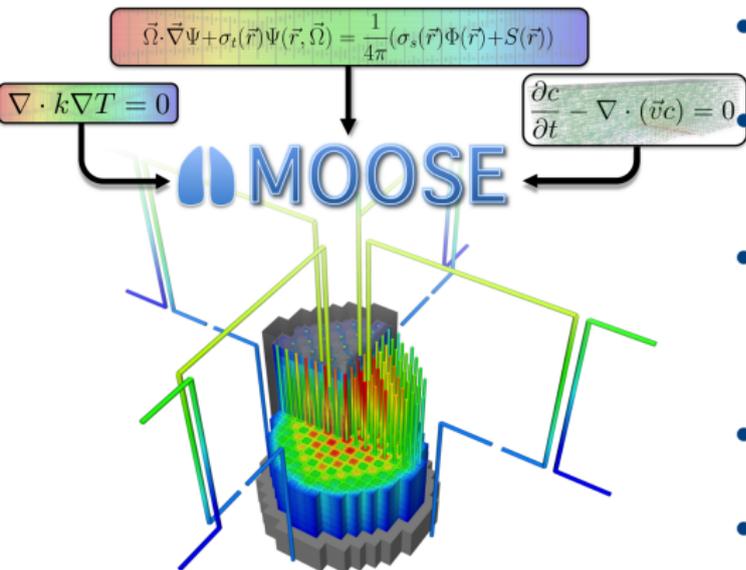
^{232}Th refill rate



- Fluctuation due to batch-wise removal of strong absorbers
- Feed rate varies due to neutron energy spectrum evolution
- ^{232}Th consumption is 100 g/GWh_e

Figure: ^{232}Th feed rate over 20 years of MSBR operation

MOOSE Framework

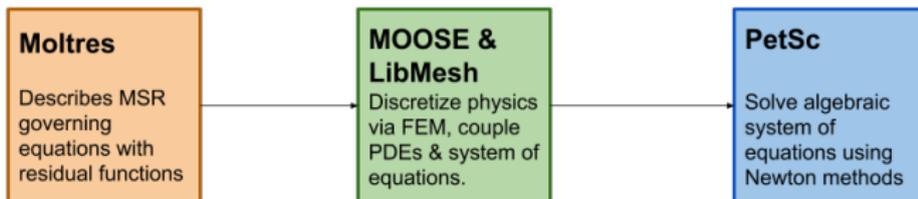


- Fully-coupled, fully-implicit multiphysics solver
- MOOSE interfaces with libMesh to discretize simulation volume into finite elements
- Residuals and Jacobians handed off to Petsc which handles solution of resulting non-linear system of algebraic equations
- Automatically parallel (largest runs >100,000 CPU cores!)
- Built-in mesh adaptivity
- Intuitive parallel multiscale solves

Figure: Multi-physics Object-Oriented Simulation Environment (MOOSE).



Moltres (Coupling in MOOSE)





Intro to Moltres

- Fluid-fuelled, molten salt reactors
- Multi-group diffusion (arbitrary groups)
- Advective movement of delayed neutron precursors
- Navier-Stokes thermal hydraulics
- 3D unstructured
- 2D axisymmetric
- 3D structured



Acquiring Moltres

```
git clone https://github.com/arfc/moltres
cd moltres
git submodule init
git submodule update
```

Diffusion in Moltres

$$\frac{1}{v_g} \frac{\partial \phi_g}{\partial t} - \nabla \cdot D_g \nabla \phi_g + \Sigma_g^r \phi_g = \quad (21)$$

$$\sum_{g \neq g'}^G \Sigma_{g' \rightarrow g}^s \phi_{g'} + \chi_g^p \sum_{g'=1}^G (1 - \beta) \nu \Sigma_{g'}^f \phi_{g'} + \chi_g^d \sum_i^I \lambda_i C_i \quad (22)$$

v_g = speed of neutrons in group g (23)

ϕ_g = flux of neutrons in group g (24)

t = time (25)

D_g = Diffusion coefficient for neutrons in group g (26)

Σ_g^r = macroscopic cross-section for removal of neutrons from group g (27)

$\Sigma_{g' \rightarrow g}^s$ = macroscopic cross-section of scattering from g' to g (28)

χ_g^p = prompt fission spectrum, neutrons in group g (29)

G = number of discrete groups, g (30)

ν = number of neutrons produced per fission (31)

Σ_g^f = macroscopic cross section for fission due to neutrons in group g (32)

χ_g^d = delayed fission spectrum, neutrons in group g (33)

I = number of delayed neutron precursor groups (34)

β = delayed neutron fraction (35)



Moltres Delayed Neutrons

$$\frac{\partial C_i}{\partial t} = \sum_{g'=1}^G \beta_i \nu \Sigma_{g'}^f \phi_{g'} - \lambda_i C_i - \frac{\partial}{\partial z} u C_i \quad (38)$$

Moltres Fuel Temperature

$$\rho_f c_{p,f} \frac{\partial T_f}{\partial t} + \nabla \cdot (\rho_f c_{p,f} \vec{u} \cdot T_f - k_f \nabla T_f) = Q_f \quad (39)$$

$$\rho_f = \text{density of fuel salt} \quad (40)$$

$$c_{p,f} = \text{specific heat capacity of fuel salt} \quad (41)$$

$$T_f = \text{temperature of fuel salt} \quad (42)$$

$$\vec{u} = \text{velocity of fuel salt} \quad (43)$$

$$k_f = \text{thermal conductivity of fuel salt} \quad (44)$$

$$Q_f = \text{source term} = \sum_{g=1}^G \epsilon_{f,g} \Sigma_{f,g} \phi_g \quad (45)$$



Moltres Moderator Temperature

$$\rho_g c_{p,g} \frac{\partial T_g}{\partial t} + \nabla \cdot (-k_g \nabla T_g) = Q_g \quad (46)$$

(47)

$$\rho_g = \text{density of graphite moderator} \quad (48)$$

$$c_{p,g} = \text{specific heat capacity of graphite moderator} \quad (49)$$

$$T_g = \text{temperature of graphite moderator} \quad (50)$$

$$k_g = \text{thermal conductivity of graphite moderator} \quad (51)$$

$$Q_g = \text{source term in graphite moderator} \quad (52)$$

(53)

Moltres MSRE Simulation

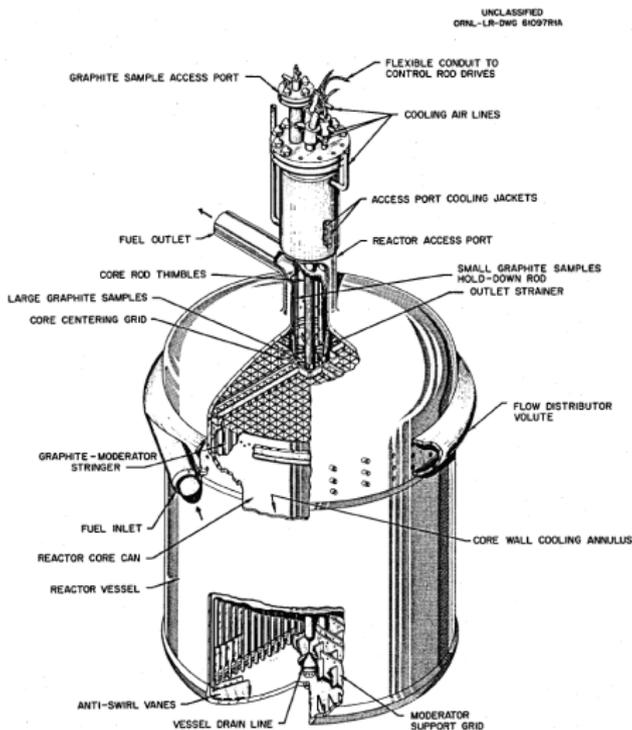


Fig. 6. MSRE Reactor Vessel.



Moltres MSRE Simulation

Table 2
 Simulation input parameters.

Parameter	Value	Units	Source
Inlet temp.	922	K	MSRE nominal (Robertson, 1965)
Wall temp.	922	K	MSRE nominal (Robertson, 1965)
Neutron groups	2	1	User
Precursor groups	6	1	User
Reactor radius	72.5	cm	≈MSRE radius (70.2 cm) (Robertson, 1965)
Reactor height	151.75	cm	User
k_f	.0553	W cm ⁻¹ K ⁻¹	Robertson (1965)
$c_{p,f}$	1967	J K ⁻¹ kg ⁻¹	Robertson (1965)
ρ_f	$2.146 \cdot 10^{-3} e^{-\alpha_f(T_f - 922)}$	kg cm ⁻³	Robertson (1965)
α_f	$2.12 \cdot 10^{-4}$	K ⁻¹	Haubenreich and Engel (1970)
k_g	.312	W cm ⁻¹ K ⁻¹	Cammi et al. (2011)
$c_{p,g}$	1760	J K ⁻¹ kg ⁻¹	Cammi et al. (2011)
ρ_g	$1.86 \cdot 10^{-3} e^{-\alpha_g(T_g - 922)}$	kg m ⁻³	Robertson (1965)
α_g	$1.8 \cdot 10^{-5}$	K ⁻¹	Haubenreich and Engel (1970)

Figure: Data used in [7].

Moltres MSRE Simulation

Table 1

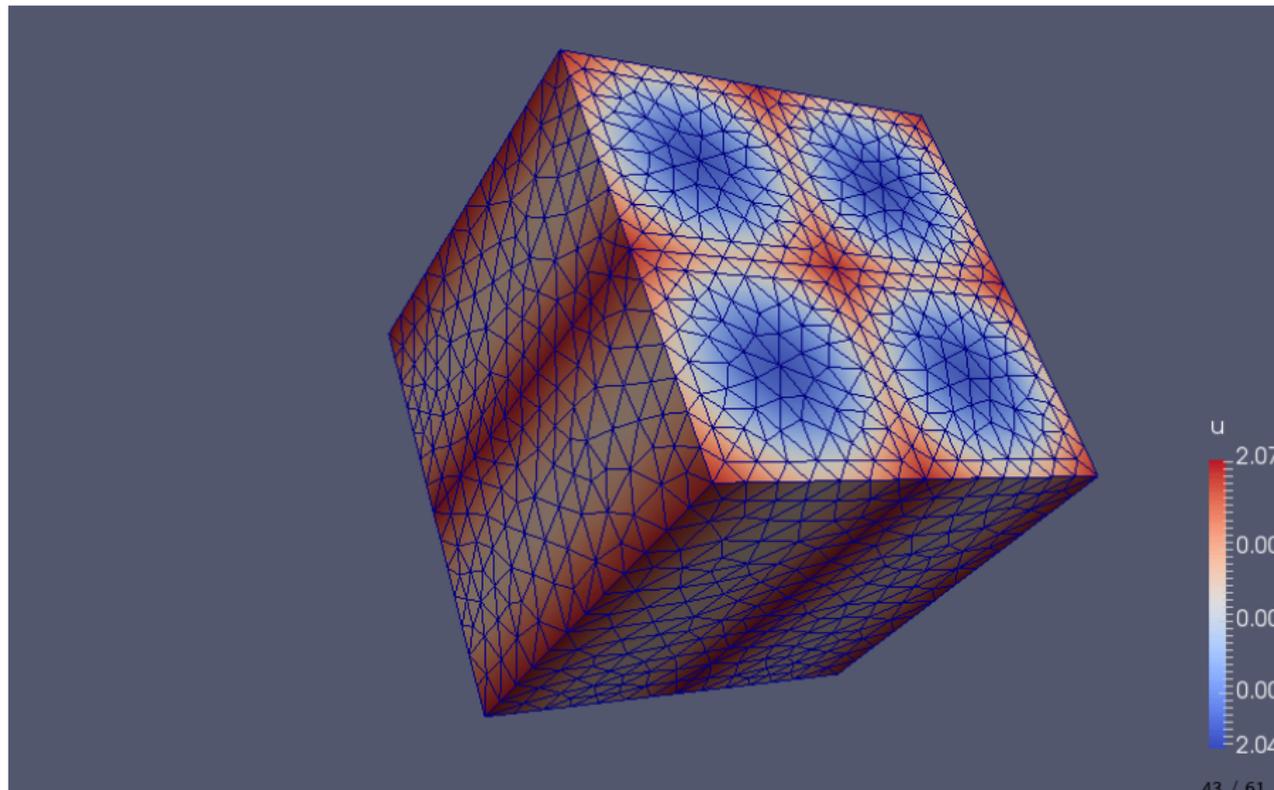
Fuel salt composition is the BOL enriched uranium composition in the MSRE design (Robertson, 1965).

Component	Mass fraction
Li-7	.1090
Li-6	5×10^{-6}
F-19	.6680
Be-9	.0627
U-235	.0167
U-238	.0344

Figure: Data used in [7].

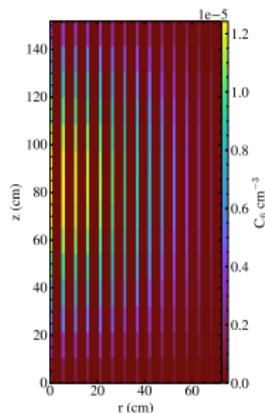
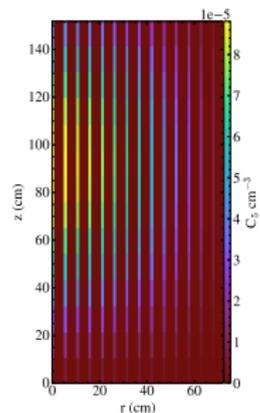
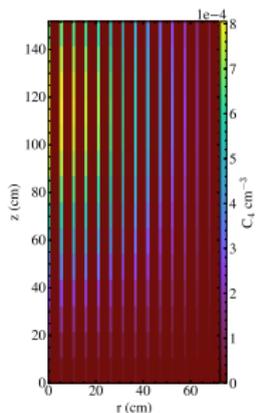
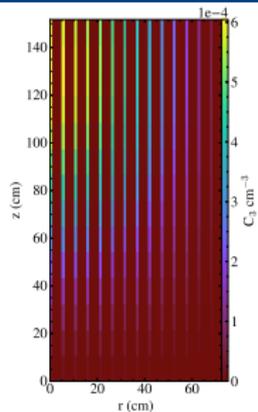
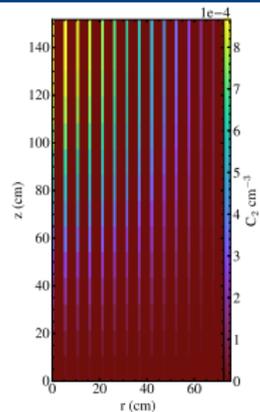
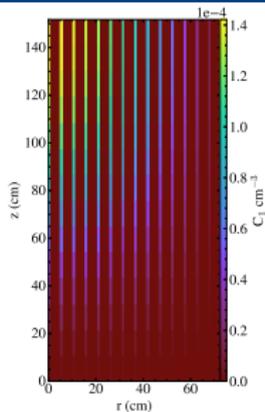


Moltres (coupling in MOOSE)





Moltres Precursor Drift



Moltres MSRE Comparison

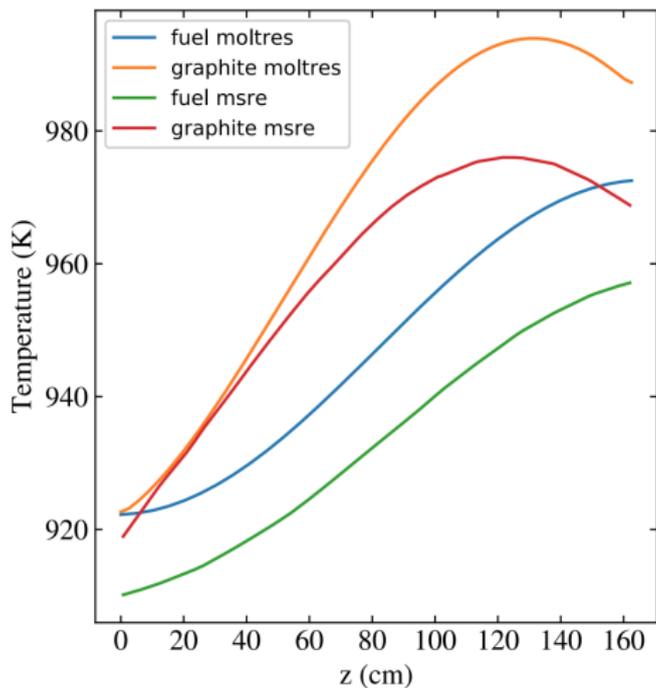


Fig. 11. Moltres and MSRE design (Briggs, 1964, p. 99) predicted axial temperature profiles in hottest channel and adjacent graphite.

Moltres MSRE Comparison

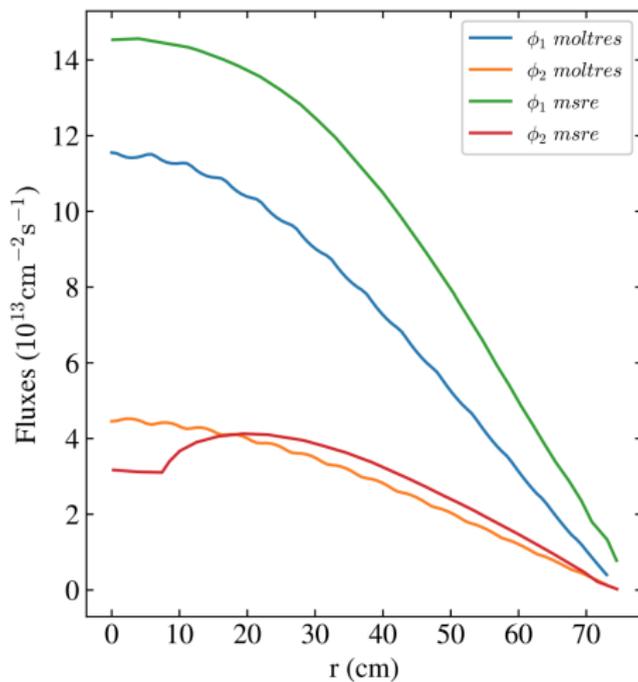


Fig. 12. The thermal and fast flux profiles at the core mid-plane ($z = H/2$) for the Moltres 2-D cylindrical axisymmetric model and the MSRE design model (Briggs, 1964, p. 92) ($r = 0$ is radial center of core).

Moltres MSRE Comparison

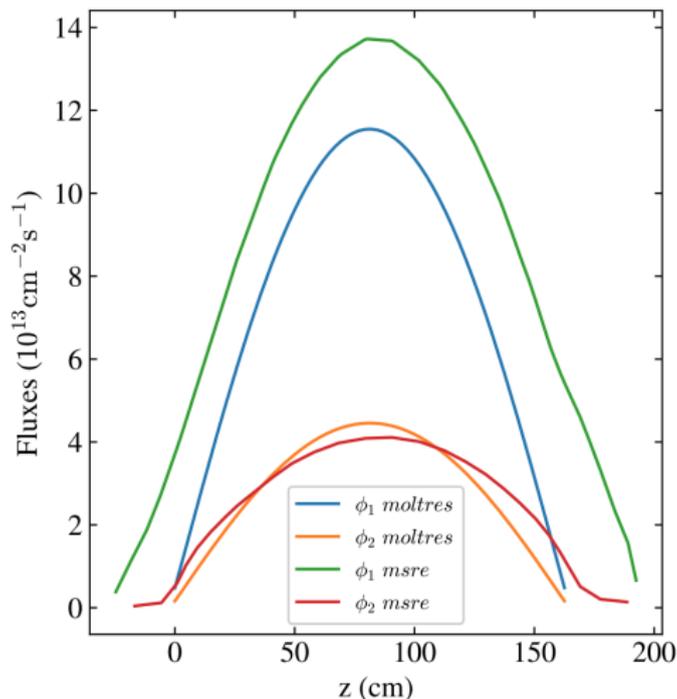


Fig. 13. Moltres axial flux profiles along the core center line and MSRE design axial flux profiles 21.336 cm (8.4 inches) from the core center line (Briggs, 1964, p. 91).

Multiphysics simulation results (3D)

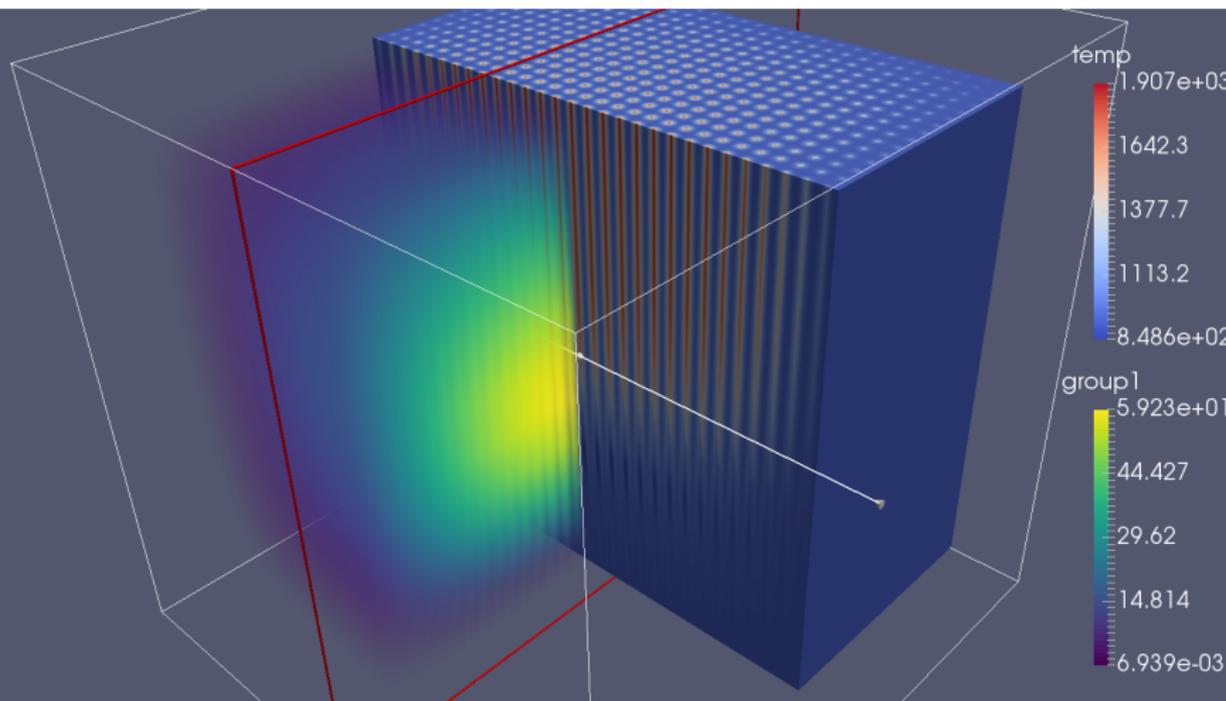


Figure: Cuboidal MSR steady-state temperature and fast neutron flux tests by Gavin Ridley.

Conclusions

Ordinary tools cannot capture kinetics in mobile fuels or long term fuel cycle performance of liquid-fuelled reactors.

SaltProc

- New tool **SaltProc** was developed to simulate fuel depletion in MSRs.
- **SaltProc** was tested for the MSBR conceptual design, equilibrium fuel salt composition was found and verified against recent studies.

Moltres

- New tool **Moltres** was developed for modeling coupled physics in novel molten salt reactors.
- 2D-axisymmetric and 3D multiphysics models are presented.
- **Moltres** demonstrated strong parallel scaling (up to 384 physical cores) but further optimization required.
- Over 55,000 node-hours were consumed on **Blue Waters** to perform this research.

Future research

Future Directions

- ① Improved TH capabilities in Moltres will enable more realistic precursor drift.
- ② Equilibrium state search for Transatomic MSR ($>30,000$ node-hours).
- ③ Fuel cycle performance analysis for load-following regime ($>40,000$ node-hours).
- ④ Light Water Reactor (LWR) fuel transmutation in MSR viability ($>30,000$ node-hours).
- ⑤ Start exploring transients in Moltres, e.g. explore responses to reactivity insertion or gaseous poison removal ($>70,000$ node-hours).

Acknowledgements

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References I

- [1] C. Andreades, A.T. Cisneros, J.K. Choi, A.Y.K Chong, David L. Krumwiede, Lakshana Huddar, Kathryn D. Huff, M.D. Laufer, Madicken Munk, Raluca O. Scarlat, Jeffrey E. Seifried, Nicolas Zwiebaum, Ehud Greenspan, and Per F. Peterson.
Technical Description of the 'Mark 1' Pebble-Bed, Fluoride-Salt-Cooled, High-Temperature Reactor Power Plant.
Thermal Hydraulics Group UCBTH-14-002, University of California, Berkeley, Department of Nuclear Engineering, Berkeley, CA, September 2014.
- [2] DOENE.
Southern Company and TerraPower Prep for Testing on Molten Salt Reactor, August 2018.
- [3] Badawy M. Elsheikh.
Safety assessment of molten salt reactors in comparison with light water reactors.
Journal of Radiation Research and Applied Sciences, 6(2):63–70, October 2013.
- [4] Charles W. Forsberg and Madeline Feltus.
Fuel requirements for the advanced high-temperature reactor: graphite coated-particle fuel and molten fluoride salt coolant.
Paper Due, 7, January 2004.

References II

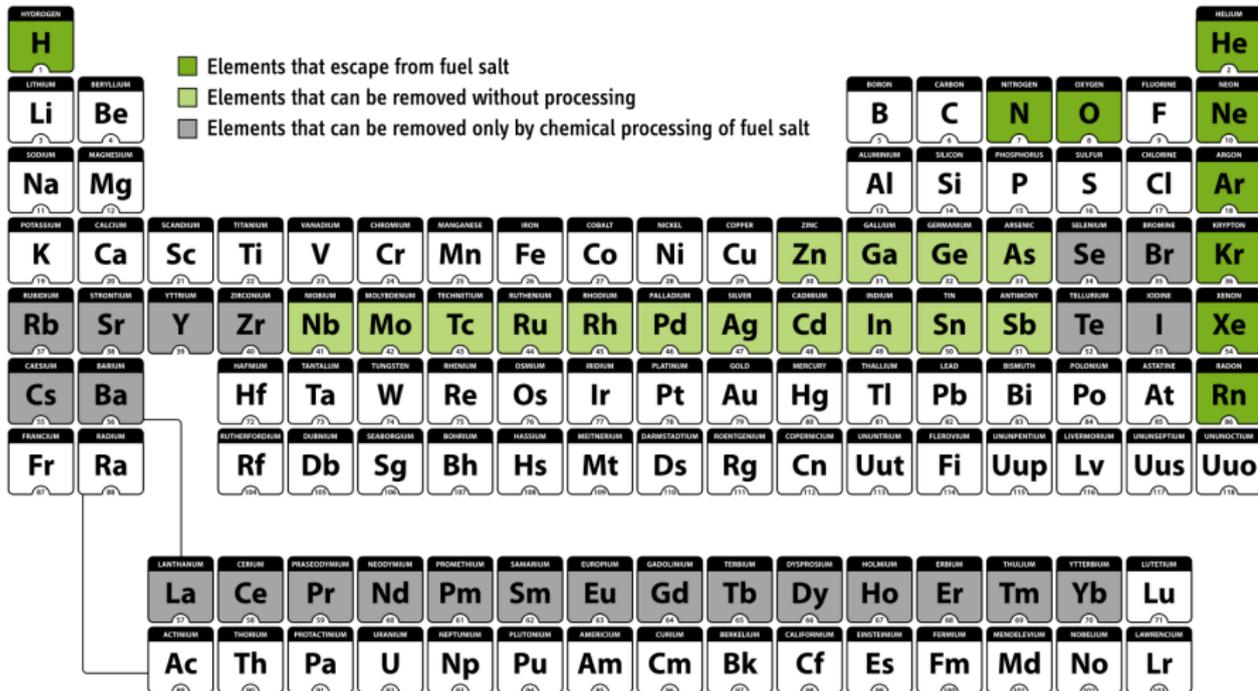
- [5] Cole Gentry, G Maldonado, and Ondrej Chvala.
Burnable Poison Reactivity Control for the Advanced High Temperature Reactor.
November 2015.
- [6] Kathryn Huff.
PyRK: Python for Reactor Kinetics, 2015.
<https://github.com/pyrk/pyrk>.
- [7] Alexander Lindsay, Gavin Ridley, Andrei Rykhlevskii, and Kathryn Huff.
Introduction to Moltres: An application for simulation of Molten Salt Reactors.
Annals of Nuclear Energy, 114:530–540, April 2018.
- [8] R. C. Robertson.
Conceptual Design Study of a Single-Fluid Molten-Salt Breeder Reactor.
Technical Report ORNL-4541, comp.; Oak Ridge National Lab., Tenn., January 1971.
- [9] M. W. Rosenthal, P. R. Kasten, and R. B. Briggs.
Molten-Salt Reactors—History, Status, and Potential.
Nuclear Applications and Technology, 8(2):107–117, February 1970.

References III

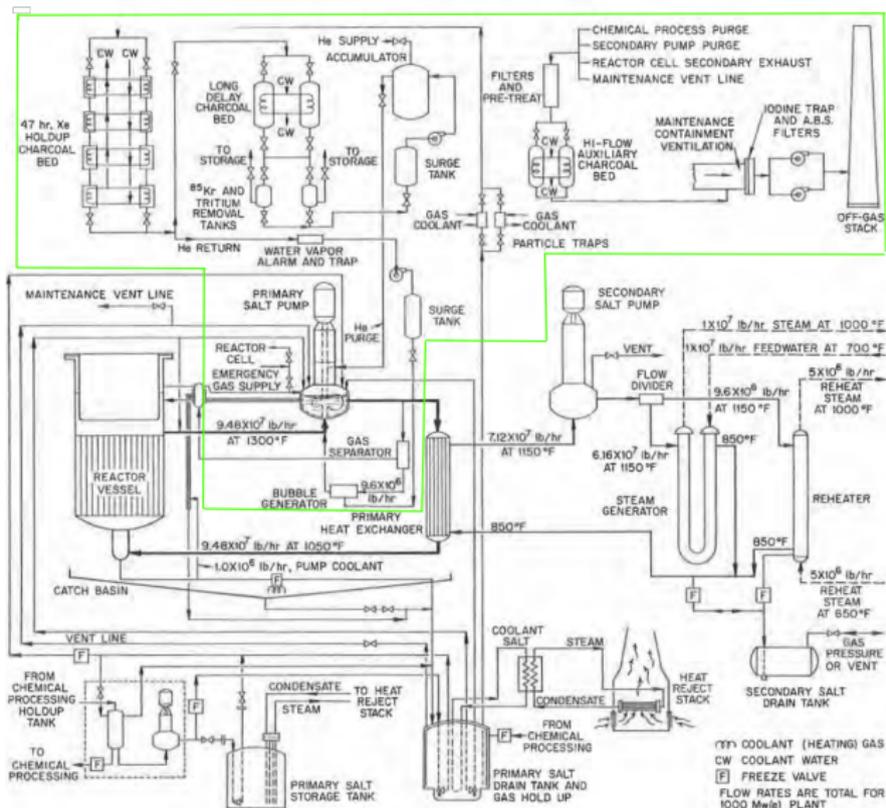
- [10] Andrei Rykhlevskii, Jin Whan Bae, and Kathryn Huff.
arfc/saltproc: Code for online reprocessing simulation of Molten Salt Reactor with external depletion solver SERPENT, March 2018.
- [11] Andrei Rykhlevskii, Alexander Lindsay, and Kathryn D. Huff.
Online reprocessing simulation for thorium-fueled molten salt breeder reactor.
In Transactions of the American Nuclear Society, Washington, DC, United States, November 2017. American Nuclear Society.
- [12] TerraPower LLC.
MCFR TerraPower, December 2018.
- [13] Xin Wang, Kathryn D. Huff, Manuele Aufiero, Per F. Peterson, and Massimiliano Fratoni.
Coupled Reactor Kinetics and Heat Transfer Model for Fluoride Salt-Cooled High-Temperature Reactor Transient Analysis.
June 2016.



Processing options for MSR fuels

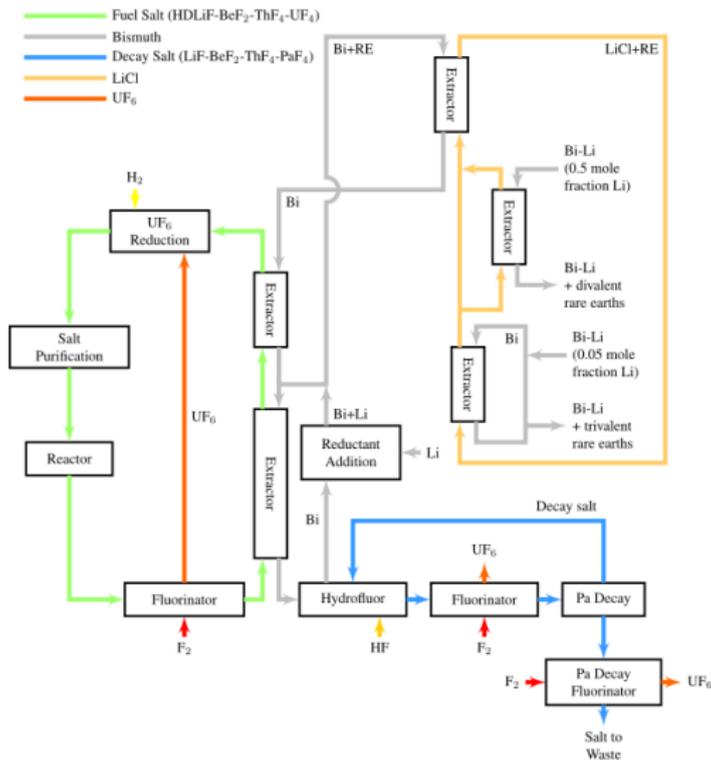


BUBBLE GENERATOR AND GAS SEPARATOR for MSBR

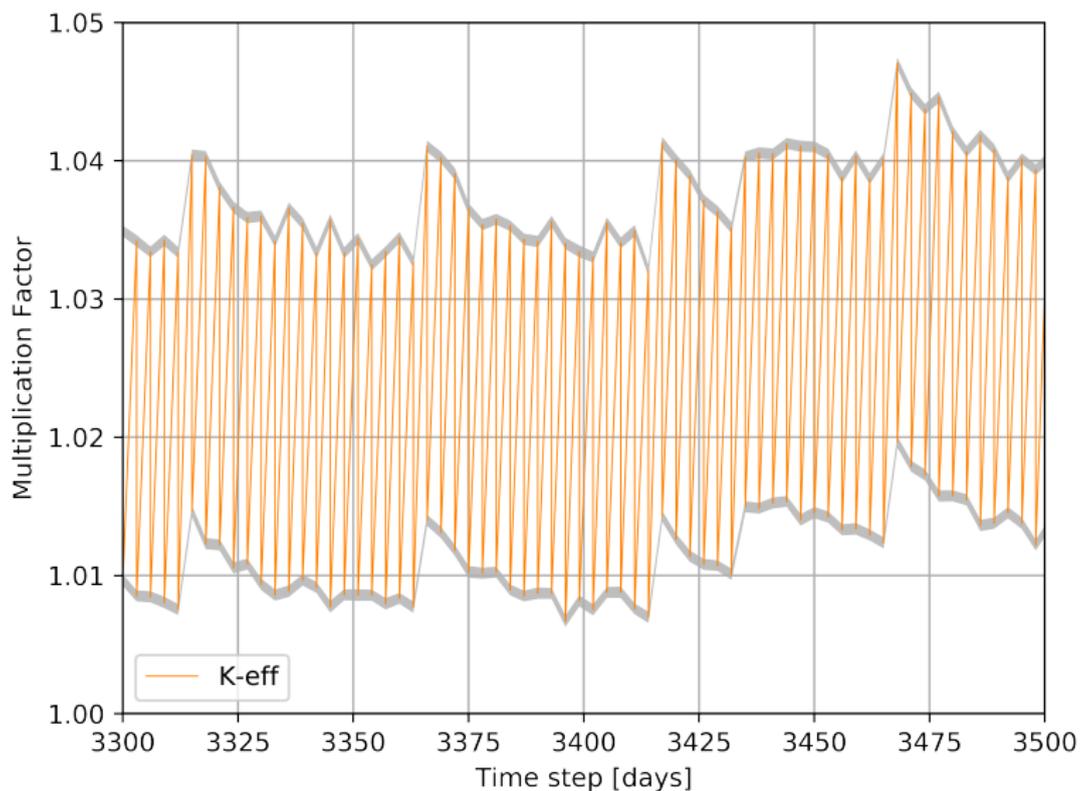




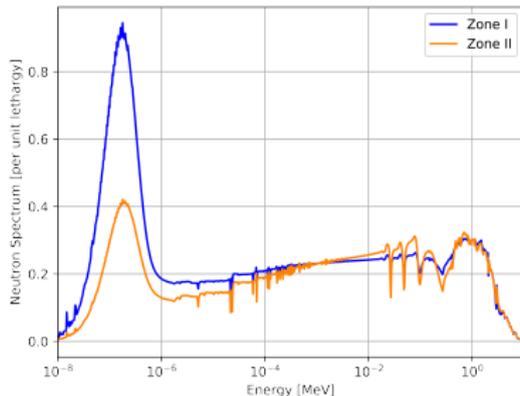
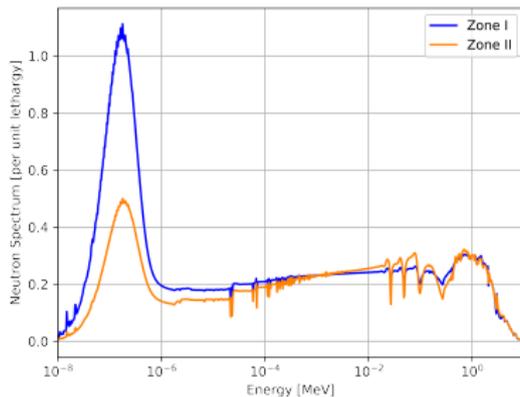
Chemical processing facility for MSBR



Multiplication factor dynamics during Rb, Sr, Cs, Ba removal (3435days)

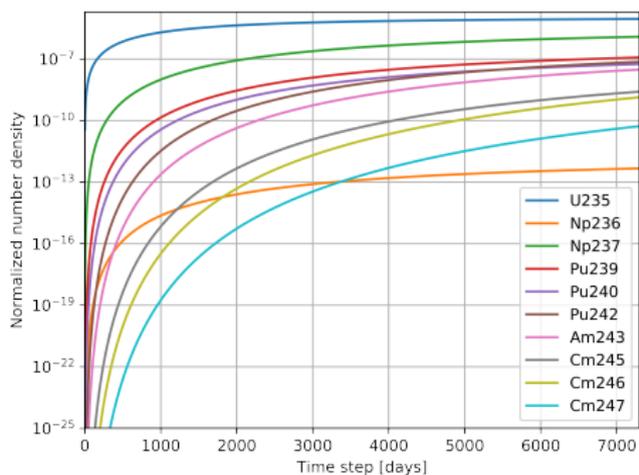
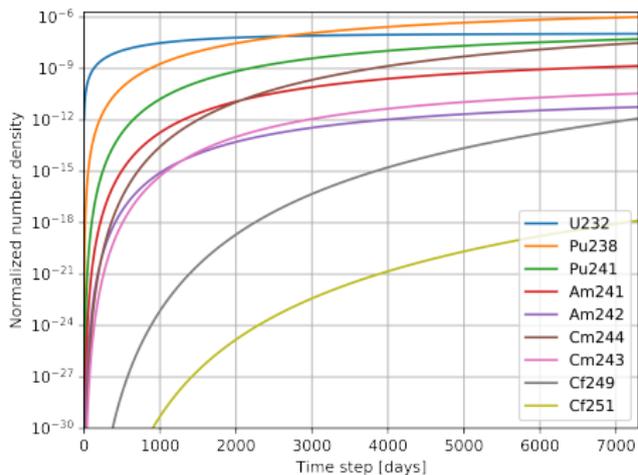


MSBR neutron energy spectrum for different regions





Fissile isotopes in the MSBR core



MSBR plain view

