Moltres: a MOOSE Application for Simulation of MSRs

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Presentation Overview

- Intro to Moltres/MOOSE
- Moltres goals
- Results:
 - 3D unstructured: temperature coupling issues
 - 2D axisymmetric: good steady-state profiles
 - 3D structured: steady-state neutron and precursor profiles; incomplete conduction between fuel and moderator
- Future work
 - Transients

Obtaining Moltres

- git clone https://github.com/arfc/moltres
- cd moltres
- git submodule init
- git submodule update

Moltres/MOOSE

- Moltres is built on top of the Multi-physics Object-Oriented Simulation Environment (MOOSE):
- MOOSE interfaces with libMesh to discretize simulation volume into finite elements
- Provides interface for coding residuals that correspond to weak form of governing PDEs; also interface for coding Jacobians → more accurate Jacobians → more efficient convergence
- Residuals and Jacobians handed off to PetSc which handles solution of resulting non-linear system of algebraic equations



CoupledFissionEigenKernel

$$-\frac{\chi_g^p}{k}\sum_{g'=1}^G(1-\beta)\nu\Sigma_{g'}^f\phi_{g'}$$

CoupledFissionKernel

$$-\chi_g^p \sum_{g'=1}^G (1-\beta)\nu \Sigma_{g'}^f \phi_{g'}$$

CoupledScalarAdvection

 $\nabla \cdot \vec{a}u$

DelayedNeutronSource

$$-\chi_g^d \sum_i^I \lambda_i C_i$$

DivFreeCoupledScalarAdvection

 $\vec{a} \cdot \nabla u$

FissionHeatSource

$$-\frac{P}{\int_{\partial V}\sum_{g'=1}^{G}\nu\Sigma_{g'}^{f}\phi_{g'}dV}\sum_{g'=1}^{G}\nu\Sigma_{g'}^{f}\phi_{g'}$$

where P is a representation of the total power of the reactor.

Moltres Kernels

- In MOOSE jargon, kernels are individual pieces of governing equations
- Modular in nature; for example, a "Diffusion" kernel could be used equally well to describe conduction or viscous shear

Moltres Kernels

PrecursorSource

$$-\sum_{g'=1}^G \beta_i \nu \Sigma_{g'}^f \phi_{g'}$$

 \sim

GammaHeatSource

$$-\gamma Q_f$$

where γ is a factor representing heat dissipation by gamma and neutron irradiation in the moderator and Q_f is given by:

$$\sum_{g=1}^G \epsilon_{f,g} \Sigma_{f,g} \phi_g$$

with $\epsilon_{f,g}$ the amount of heat given off per fission event.

GroupDiffusion

$$-\nabla \cdot D_g \nabla \phi_g$$

InScatter

$$-\sum_{g\neq g'}^G \Sigma^s_{g'\rightarrow g} \phi_{g'}$$

NtTimeDerivative

$$\frac{1}{v_g} \frac{\partial \phi_g}{\partial t}$$

PrecursorDecay

 $\lambda_i C_i$

ScalarAdvectionArtDiff

$$\nabla \cdot -\delta \nabla u$$

where δ is an artificial diffusion coefficient determined by:

$$\delta = \frac{|\vec{a}|h_{max}}{2}$$

with \vec{a} the advection velocity and h_{max} the maximum element length dimension.

ScalarTransportTimeDerivative

$$\frac{\partial u}{\partial t}$$

SelfFissionEigenKernel

$$\frac{-\nu_f \Sigma_f \phi}{k}$$

 $\Sigma_g^r \phi_g$

SigmaR

TransientFissionHeatSource

$$-\sum_{g=1}^G \epsilon_{f,g} \Sigma_{f,g} \phi_g$$

Governing Equations

- Piece together the kernels:
 - Multi-group diffusion
 - Precursor balance with drift
 - Heat conduction-convection with fission source in fuel
 - Heat conduction with option for irradiation source in moderator

$$\frac{1}{v_g} \frac{\partial \phi_g}{\partial t} - \nabla \cdot D_g \nabla \phi_g + \Sigma_g^r \phi_g = \sum_{g \neq g'}^G \Sigma_{g' \to g}^s \phi_{g'} + \chi_g^p \sum_{g'=1}^G (1-\beta) \nu \Sigma_{g'}^f \phi_{g'} + \chi_g^d \sum_i^I \lambda_i C_i$$
$$\frac{\partial C_i}{\partial t} = \sum_{g'=1}^G \beta_i \nu \Sigma_{g'}^f \phi_{g'} - \lambda_i C_i - \frac{\partial}{\partial z} u C_i$$
$$\rho_f c_{p,f} \frac{\partial T_f}{\partial t} + \nabla \cdot (\rho_f c_{p,f} \vec{u} \cdot T_f - k_f \nabla T_f) = Q_f$$
$$\rho_g c_{p,g} \frac{\partial T_g}{\partial t} + \nabla \cdot (-k_g \nabla T_g) = Q_g$$

Example Literature MSR Multi-Physics

- Cammi Ann. of Nuc. Energy 38 (2011) 1356
- Single channel
- Reflective/insulating conditions at radial boundary for neutrons/temperature
- Variables: velocity (ur, uz), fluxes (2 group), temperature, precursor conc.



Concurrent efforts in Italy, Switzerland, DOE lab, UCB, and others

Goals

- Current:
 - demonstrate steady-state coupling of neutron fluxes, precursors, and temperature for thermal MSR design
- Future:
 - investigate reactor dynamics under transient accident scenarios to assess safety
 - explore salt processing and chemistry

Problem Set-Up

- Base current model on Molten Salt Reactor Experiment
- 22.5% volume fraction fuel
- Remainder graphite
- Fuel salt: Fluoride Lithium Beryllium (FLiBe) with 33% enriched Uranium
- Generate group constants with Serpent or Newt
- Moltres builds neutronics with action so accepts arbitrary number of groups; however, all results presented here will be for two groups

| Component | Mass Fraction |
|-----------|---------------|
| Li-7 | .1090 |
| Li-6 | 5E-6 |
| F-19 | .6680 |
| Be-9 | .0627 |
| U-235 | .0167 |
| U-238 | .0344 |



3D Geometry

- Start with simple cuboid lattice
- Red regions fuel
- 5 cm pitch



Mesh Construction

 Repeating structure, block and boundary IDs, generated using gmsh



```
or xindex In {1:num_cells-1}
new_f_surface = Translate {xindex*pitch, 0, 0} {
    Duplicata { Surface{11}; }
  };
  fuel_surfaces += new_f_surface;
  new_m_surface = Translate {xindex*pitch, 0, 0} {
    Duplicata { Surface{12}; }
  };
  moder_surfaces += new_m_surface;
EndFor // xindex
```

k-eigenvalue simulation; reactor axial mid-plane



T = 922 K; k = 1.002

Issues when Coupling in Temperature



Moderator temperatures next to highest fissioning fuel regions drop below inlet temperature of 922 K

Boundary Shocks



 Over 1 million elements in simulation, but only one internal node spans radial moderator dimension



Boundary Shocks

 Can see identical phenomena in simple Transient-Diffusion problem with quickly ramped boundary values

Moving Forward

- Move to simplified 2D-axisymmetric formulation, using same group constants and maintaining correct fuelmoderator volume fractions
- Structured mesh: allows much finer meshing in radial direction where gradients are much larger
- Return later to 3D problem, again using structured mesh



Results (neutrons)



Results (temperature)



Results (precursors)





New 3D Results

- Lessons learned from 2D-axisymmetric case: using *structured* 3D mesh, can evolve close to steady-state without observing boundary shocks
- Over heat conduction time scales, convergence slow
 - Unsure why
- Simulation run on 160 processors on Illinois's Blue Waters supercomputer

Results (neutrons)



Results (temperature)



- Not simulated out to long enough times for heat to finish conducting from fuel to moderator
- End time = 17 seconds
- Characteristic diffusion time through moderator = 24 seconds

Results (precursors)



Longest lived precursor



Shortest lived precursor

Moltres Summary/Future Work

- Good coupling with fine meshing in 2D
- Some good 3D results; slow convergence at long time scales
- Next:
 - Instead of assuming constant, couple in flow variables
 - Start exploring transients, e.g. explore responses to reactivity insertion
 - Implement cross section dependence on control rods

Moltres Summary/Future Work

- Presented preliminary results
- Still a bit to go to replicate state-of-theart multi-physics simulation capabilities
- However, we hope use of modern development practices will accelerate growth and assist in review and transparency

MOLTRES WIKI

GitHub with Continuous Integration



User guide pages

When learning Moltres and the underlying MOOSE framework, it may be best to start with a tutorial and examples.

The following pages give the math behind the Kernel and BC classes that are used to construct the weak forms of the PDEs required for the finite element method:

The page below gives a detailed outline of a typical Moltres input file and should help the user prepare his/her own customized input:

Wiki with User Guides



Doxygen pages for helping new developers

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